1-1-2012

Review: An Operator Approach to the Rational Solutions of the Classical Yang-Baxter Equation

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MR2674841 (2012c:16112) 16T25 (81R12)

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An operator approach to the rational solutions of the classical Yang-Baxter equation. (English summary)

Rep. Math. Phys. **65** (2010), *no. 2,* 165–187.

The authors study the rational solutions of the Classical Yang-Baxter Equation following the operator approach pioneered by M. A. Semenov-Tyan-Shanskiĭ [Funktsional. Anal. i Prilozhen. **17** (1983), no. 4, 17–33; MR0725413 (85i:58061)] and B. A. Kupershmidt [J. Nonlinear Math. Phys. **6** (1999), no. 4, 448–488; MR1722068 (2001a:17023)]. They provide explicit constructions and pose questions for further work. The paper is well-motivated and clearly written.

Reviewed by *Gizem Karaali*

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Note: This list reflects references listed in the original paper as accurately as possible with no attempt to correct errors.